



# Bachelor in Physics (Academic Year 2022-23)

<b>Differential Geometry and Tensor Calculus</b>			<b>Code</b>	800522	<b>Year</b>	3rd	<b>Sem.</b>	2nd
<b>Module</b>	Transversal	<b>Topic</b>	Transversal topics		<b>Character</b>	Optional		

	Total	Theory	Exercises
<b>ECTS Credits</b>	6	4	2
<b>Semester hours</b>	45	30	15

Learning Objectives (according to the Degree's Verification Document)
<ul style="list-style-type: none"> <li>• Acquire skills in different transversal subjects to be able to apply them in fourth-year courses.</li> <li>• Develop the ability to apply the concepts and methods of differential geometry and tensor calculus to problems of classical and quantum physics.</li> </ul>
Brief description of contents
Differential geometry, tensor calculus and their applications to physics.
Prerequisites
Algebra, calculus of one and several variables, and differential equations.

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Theory/Exercises – Schedule and Teaching Staff							
Group	Lecture Room	Day	Time	Professor	Period/Dates	Hours	Dept.
B	2 4A	Tu Th	13:30-15:00 18:00–19:30	Gabriel Álvarez Galindo	Full term	45	FT

Office hours				
Group	Professor	Schedule	E-mail	Location
B	Gabriel Álvarez Galindo	Tu, We: 8:00-9:00, 11:00-13:00	<a href="mailto:galvarez@fis.ucm.es">galvarez@fis.ucm.es</a>	Office 02.0317.0

Syllabus
<ol style="list-style-type: none"> <li><b>Theory of curves</b> The concept of a curve. Arc length. Curvature and torsion. Formulas of Frenet.</li> <li><b>Surfaces: first fundamental form and tensor calculus</b> The concept of a surface. Curves on a surface. First fundamental form. The concept of Riemannian geometry. Covariant and contravariant vectors. Foundations of tensor calculus. Special tensors.</li> </ol>

<p><b>3. Surfaces: second fundamental form, gaussian and mean curvature</b>                  Second fundamental form. Principal curvatures, mean and Gaussian curvature. Formulas of Weingarten and Gauss. Properties of the Christoffel symbols. The Riemann curvature tensor. Theorema egregium (Gauss).</p> <p><b>4. Geodesic curvature and geodesics</b>                  Geodesic curvature. Geodesics. Arcs of minimum length: introduction to the calculus of variations. Theorem of Gauss-Bonnet.</p> <p><b>5. Covariant differentiation and parallel transport</b>                  Covariant differentiation. The Ricci identity. The Bianchi identities. Parallel transport.</p>
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Bibliography
<ul style="list-style-type: none"> <li>• E. Kreyszig, <i>Differential Geometry</i>, Dover (1991).</li> <li>• B.A. Dubrovin, A.T. Fomenko, S.P. Novikov, <i>Modern Geometry—Methods and Applications (Part I. The Geometry of Surfaces, Transformation Groups, and Fields)</i>, Springer (1992).</li> </ul>

Online Resources
Virtual Campus.

Methodology
<p>The following learning activities will be developed:</p> <ul style="list-style-type: none"> <li>• Theory lessons, in which the fundamental concepts of the subject will be explained and illustrated with examples and applications.</li> <li>• Practical problem-solving sessions.</li> </ul> <p>The theory lessons and problem-solving sessions will take place mainly on the blackboard, although they may be supplemented with computer projections.</p> <p>The teacher will assist the students at the specified office hours in order to solve doubts or expand concepts.</p> <p>A collection of problems will be made available to students in the Virtual Campus prior to their resolution in class.</p>

Evaluation Criteria		
<b>Exams</b>	<b>Weight:</b>	70%
Grade obtained in the final exam, which will consist of theoretical questions and problems of similar difficulty to those solved in class.		
<b>Other Activities</b>	<b>Weight:</b>	30%
Exercises handed in throughout the course or carried out during classes.		
Final Mark		
<p>The final grade FG obtained by the student will be calculated by applying the following formula:</p> $FG = \max(E, 0.7E + 0.3A),$ <p>where E and A are the grades obtained in the final exam and in the “other activities”, respectively, both in the interval 0–10. The grade in the extraordinary call for June-July will be obtained following the same evaluation procedure.</p> <p>In order to compensate the exam grade E with the points obtained with “other activities”, E must be greater than 4.5 points.</p>		