



# Controlling topologically protected states by external fields and doping



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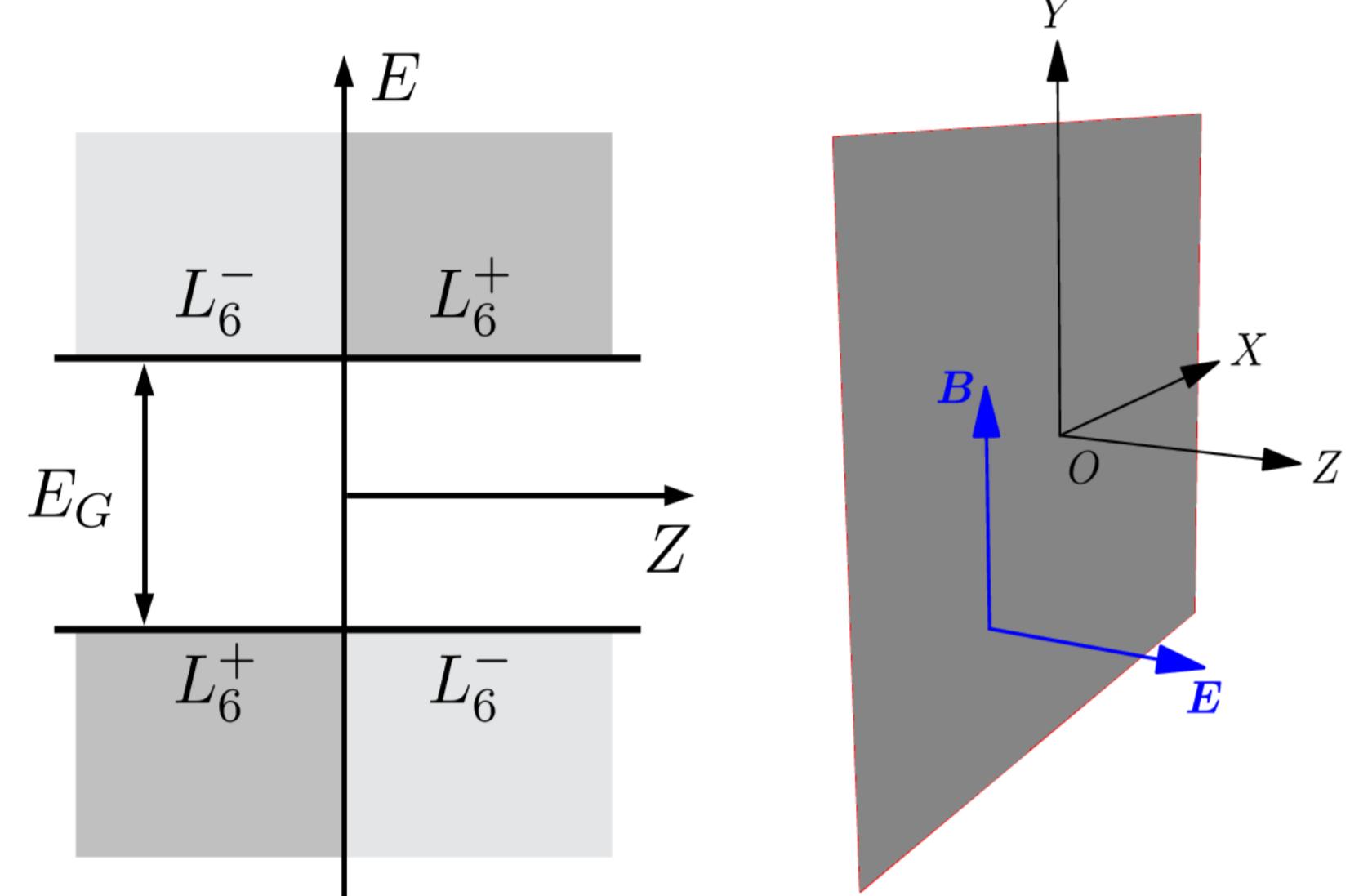
**Motivation:** Topologically protected surface states are foreseen to boost and reshape the current paradigm of electronics, spintronics, photonics and many other areas alike. It is therefore desirable to have a full control of their defining properties.

**Systems:** Three-dimensional topological insulators (e.g.  $\text{Bi}_2\text{Se}_3$ ) and topological crystalline insulators (e.g. SnTe).

**Main Results:** External electric and magnetic fields allow to dynamically modify the Fermi velocity.  $\delta$ -doping induces a coexistence between a Rashba 2DEG and the topological surface states, altering the optical transitions.

## Topological Boundary

### External Fields



### Spinful Two-Band Model

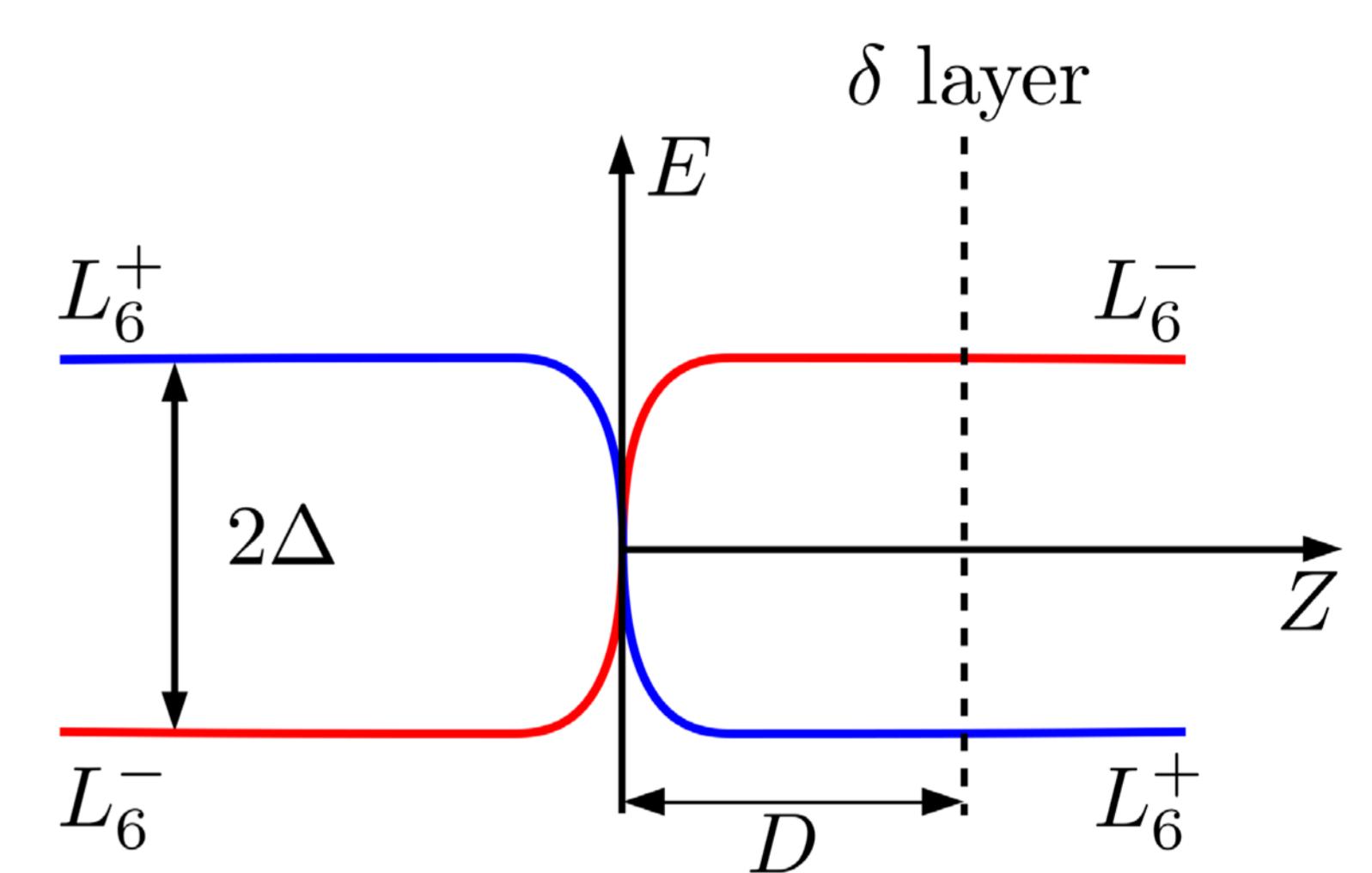
$$H = v_F \boldsymbol{\alpha} \cdot \boldsymbol{p} + \Delta(z)\beta + V(z)$$

Basis:  $|\psi\rangle \in \mathcal{H}_{\text{orbital}} \otimes \mathcal{H}_{\text{spin}}$

Bulk Symmetries:  $\mathcal{T}, \mathcal{P}$

$\mathbb{Z}_2$  topological index:  $\nu = \text{sgn}(\Delta)$

### Doping



## External Fields

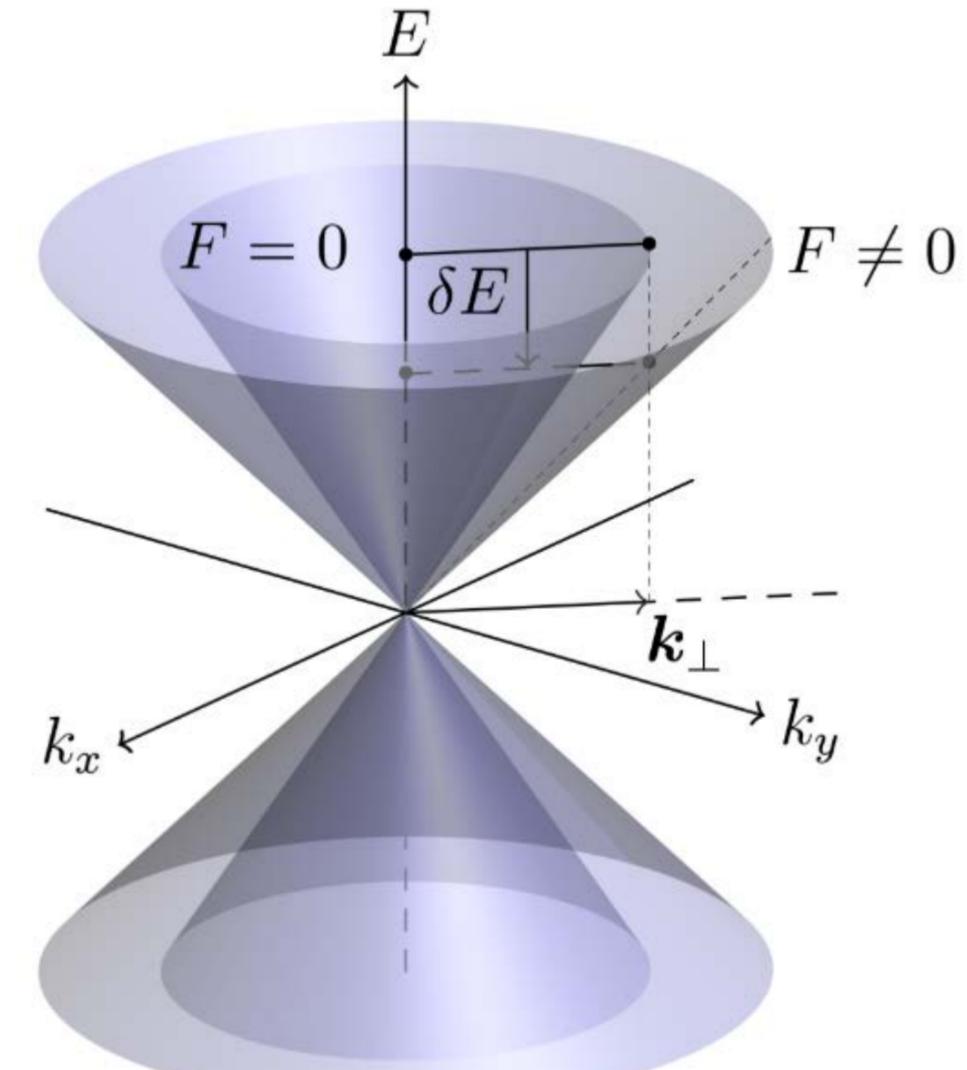
### Electric Field

Isotropic Fermi velocity reduction

$$\frac{v_F(F)}{v_F(0)} = 1 - \frac{5}{8} \frac{F^2}{F_C}$$

$$eF_C d = \Delta$$

$$d = \frac{\hbar v_F}{\Delta}$$

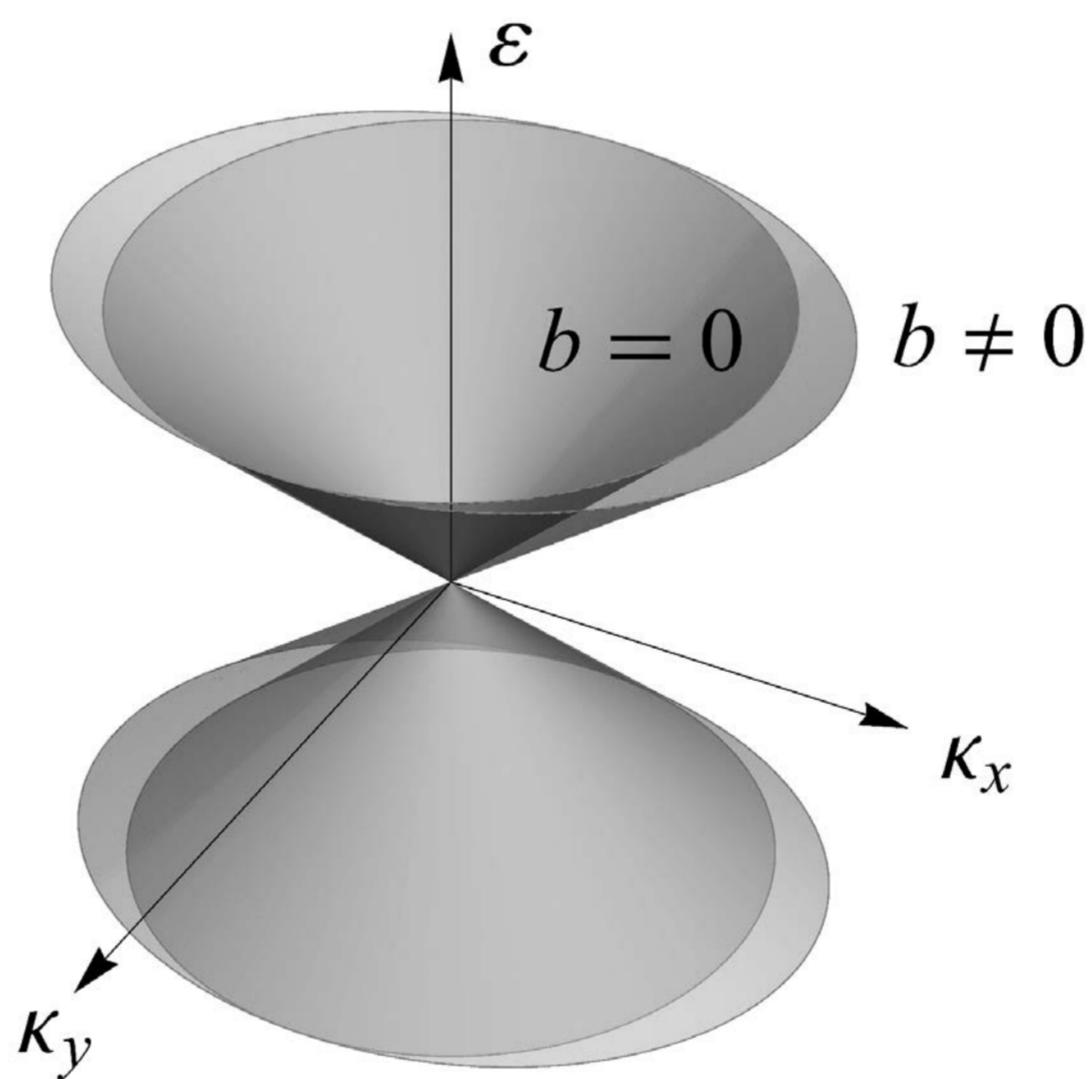


### Magnetic Field

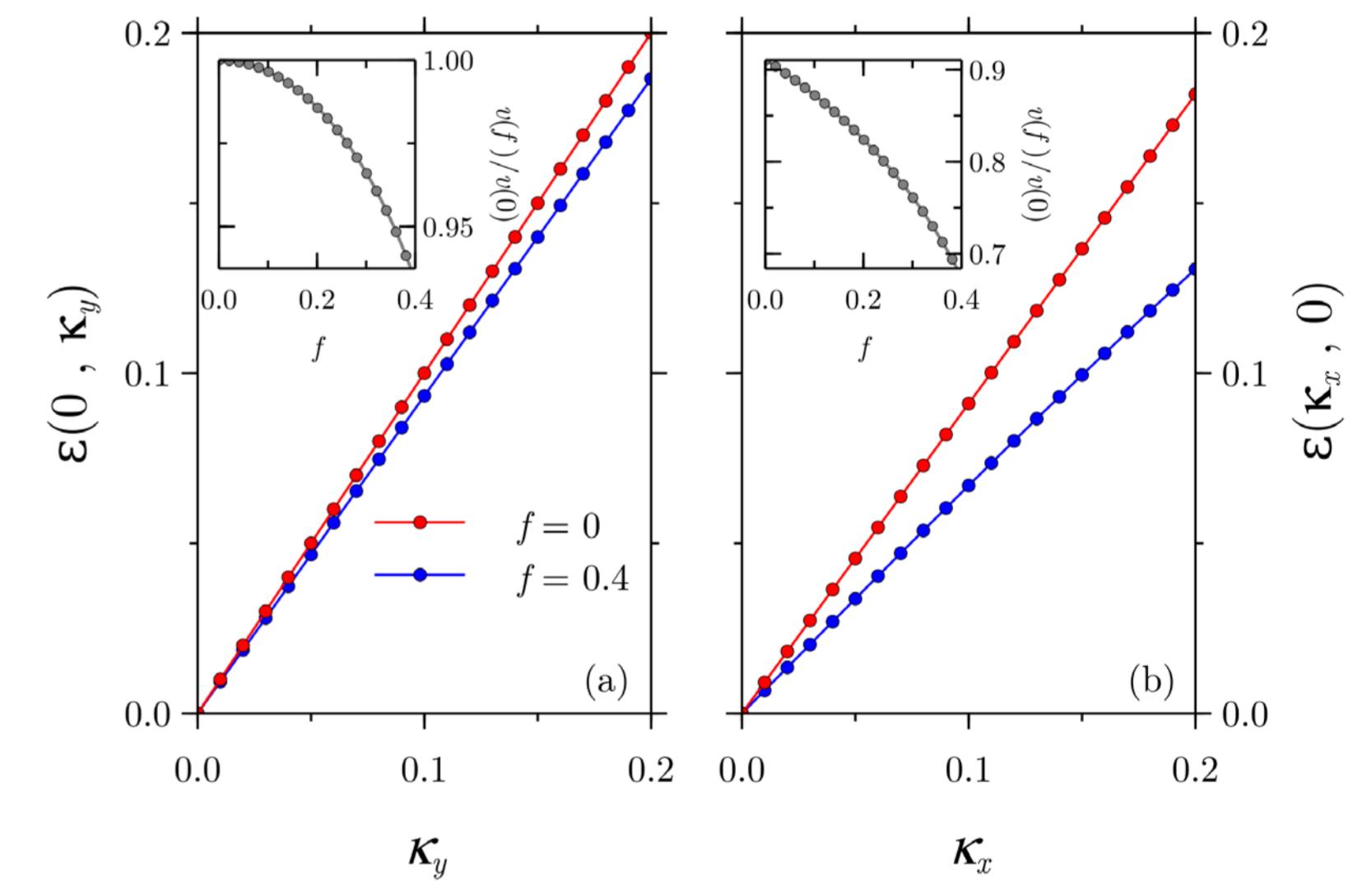
Anisotropic Fermi velocity reduction

$$\frac{v_F^x(B)}{v_F^x(0)} = 1 - \frac{5d^2}{\ell_B^2}$$

$$\ell_B = \sqrt{\frac{\hbar}{eB}}$$

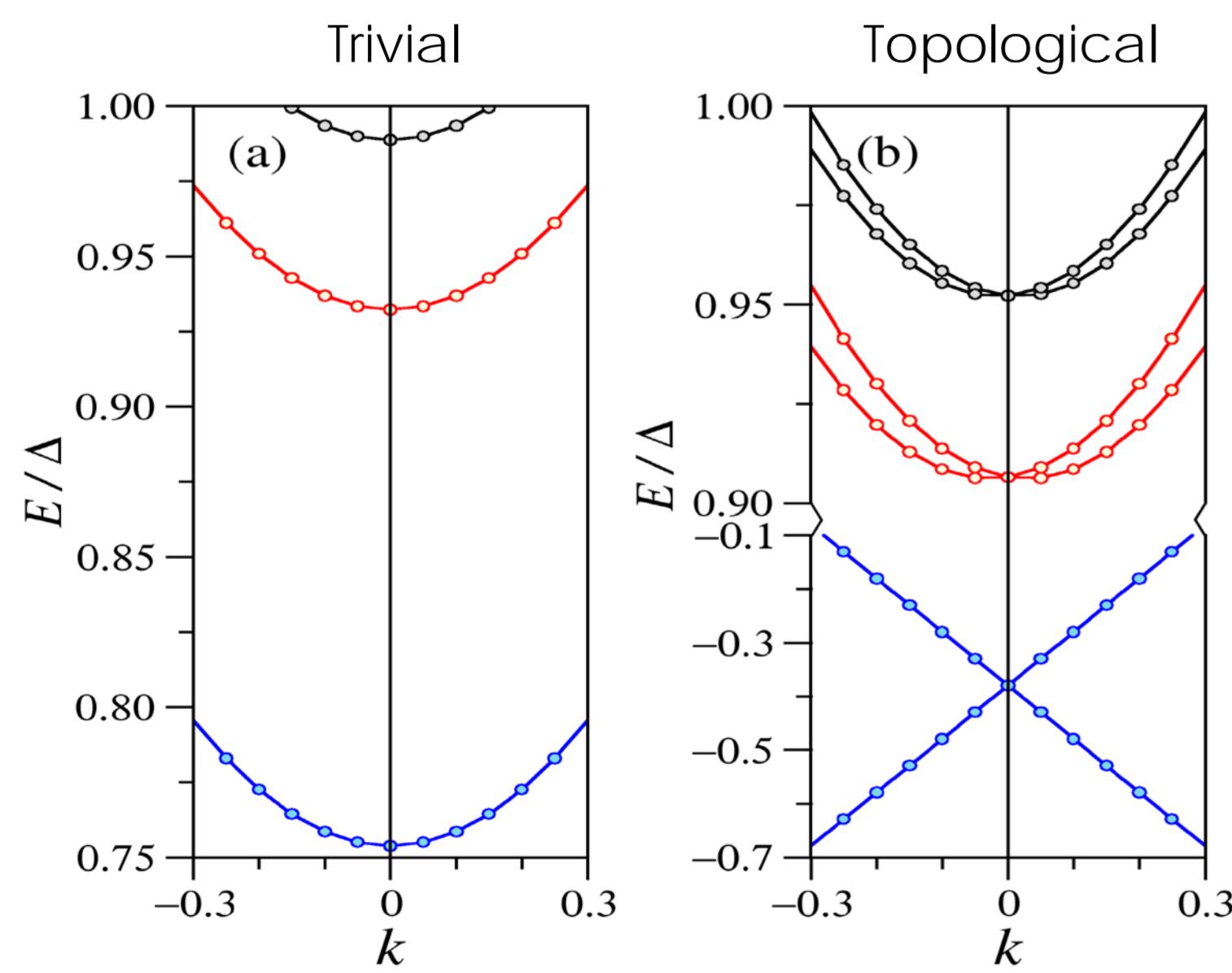


### Crossed Fields

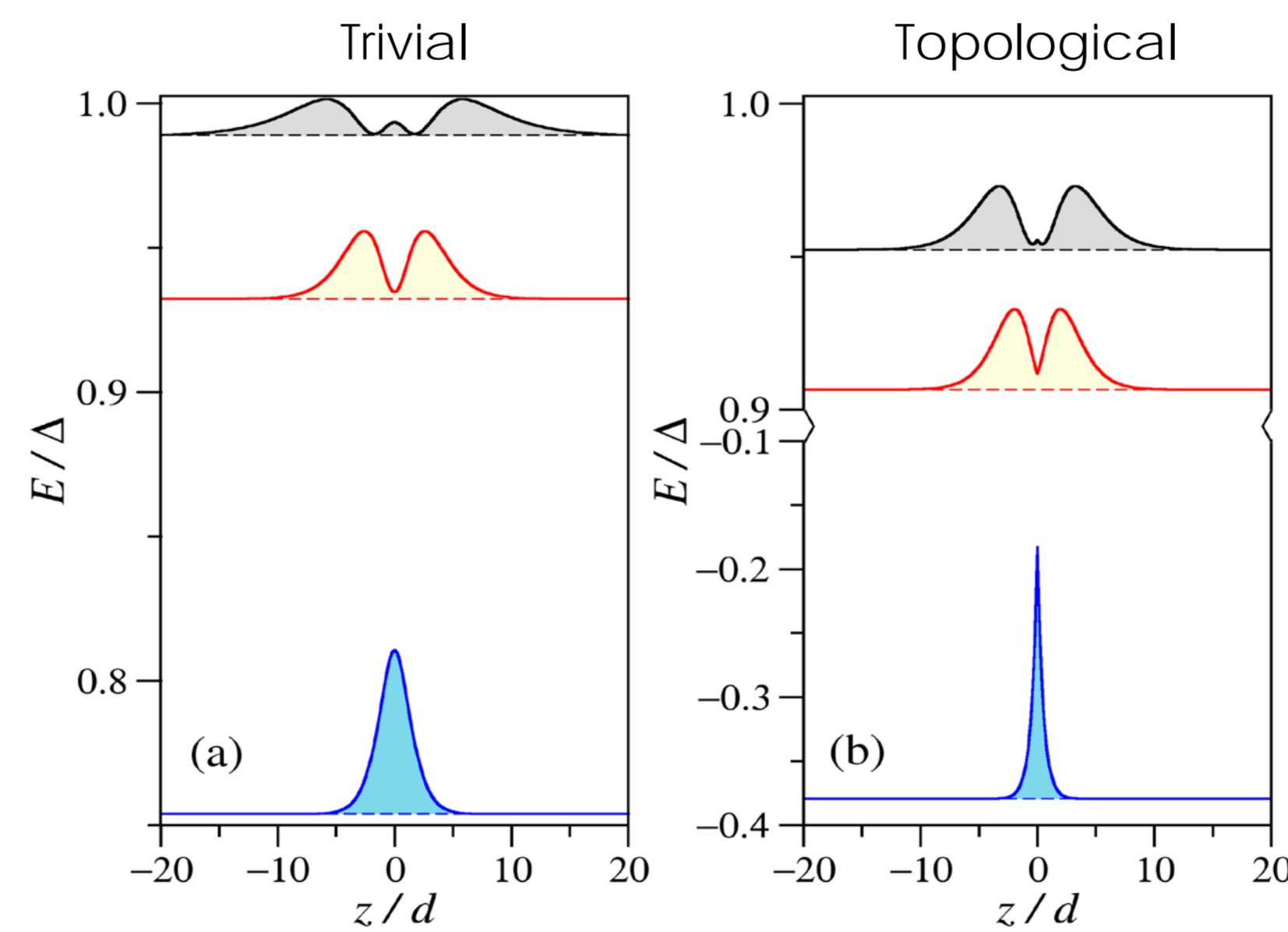


## $\delta$ -doping

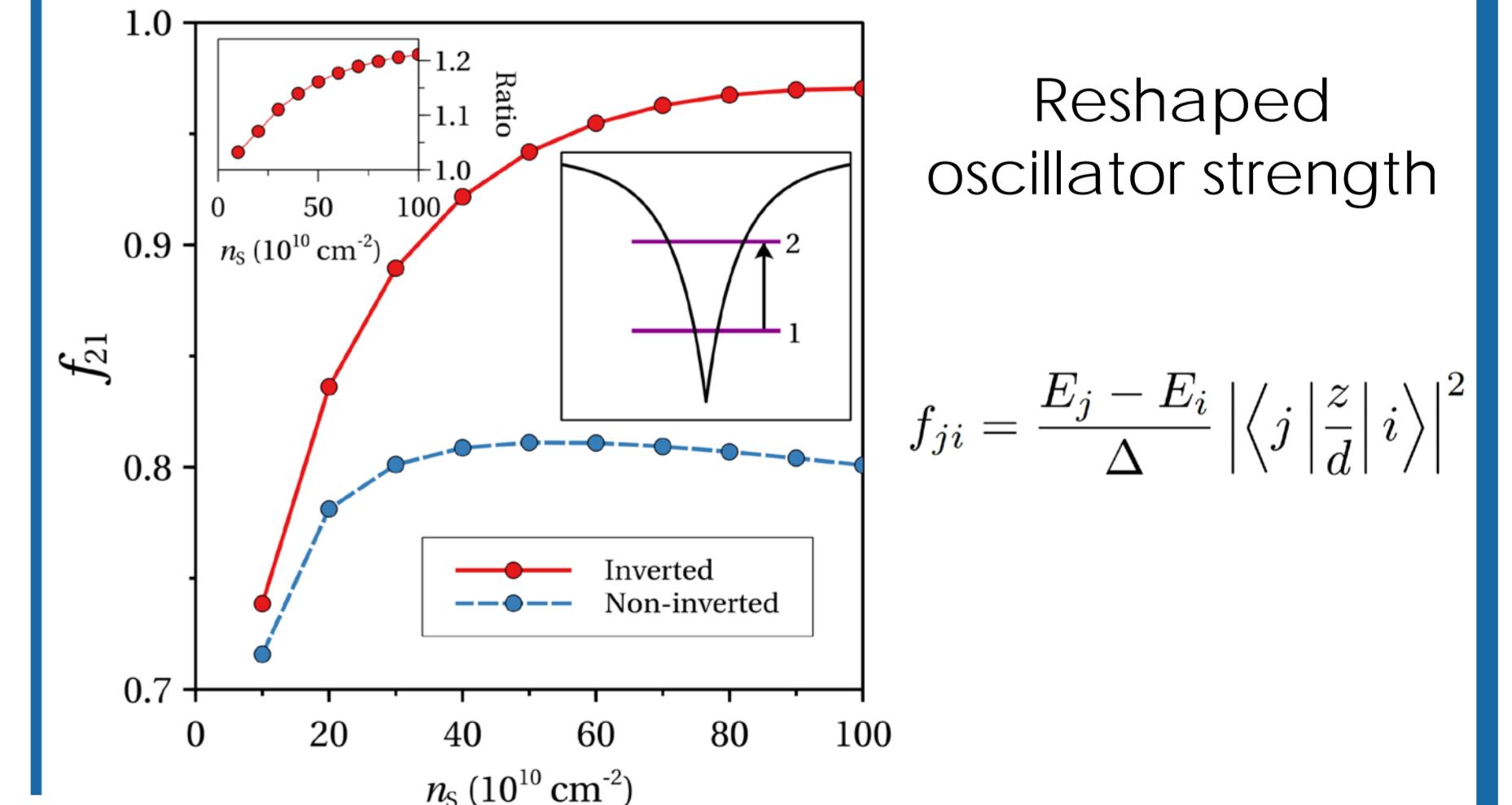
### Spectrum



### States



### Optical Transitions



## Conclusions

- Topological surface states are robust against perturbations.
- Dirac dispersion can be modified externally.
- Rashba-like 2DEG coexists with topological surface state.
- Linear optical response is reshaped by the topological state.

## References

### Topological Boundary:

- Volkov and Pankratov, JETP Lett. **42**, 178 (1985)
- F. Zhang et al., PRB **86**, 081303 (2012)

### External Fields:

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- A. Díaz-Fernández et al., Physica E **93**, 230 (2017)
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### $\delta$ -doping:

- A. Díaz-Fernández et al., PRB **98**, 085424 (2018)